

Mediation Analysis: A Case-Study

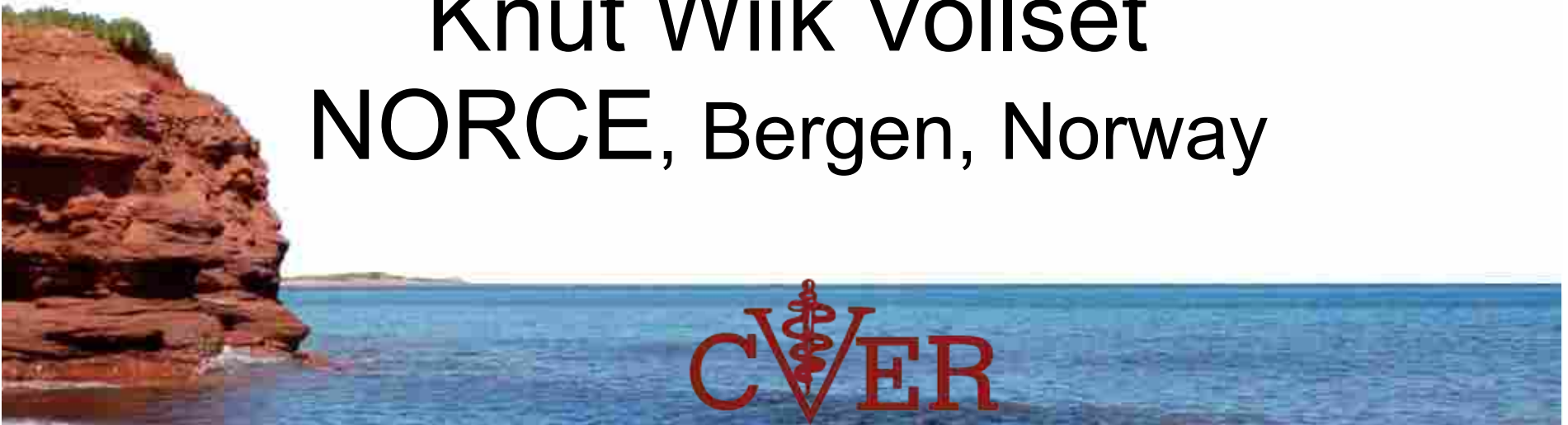
Ian Dohoo

Javier Sanchez

University of PEI, Charlottetown, Canada

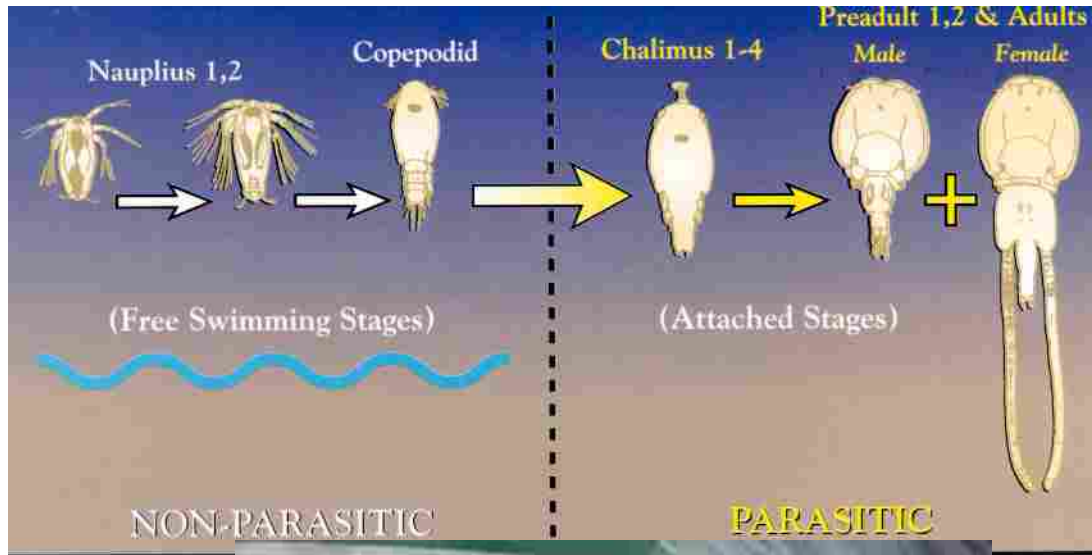
Knut Wiik Vollset

NORCE, Bergen, Norway



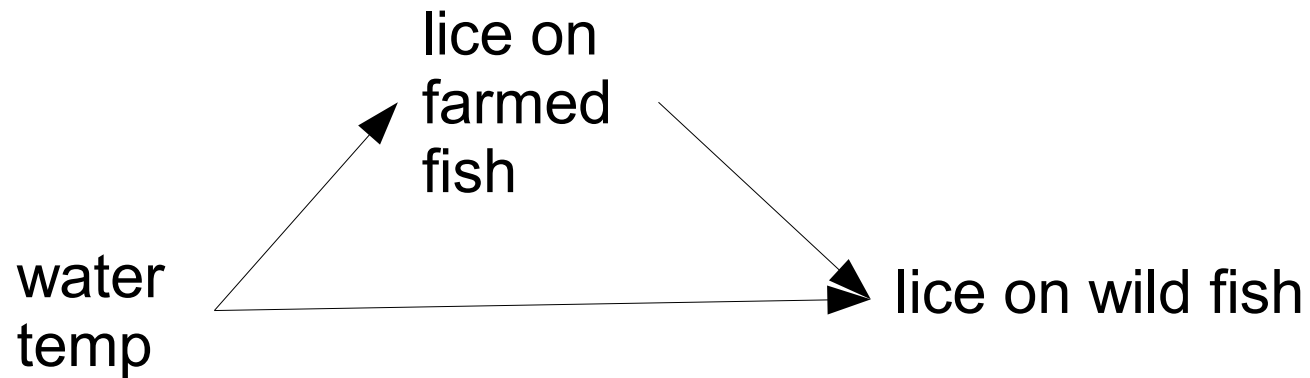
Sea Lice on Salmon

- *Lepeophtheirus salmonis*



VE

Motivating Example



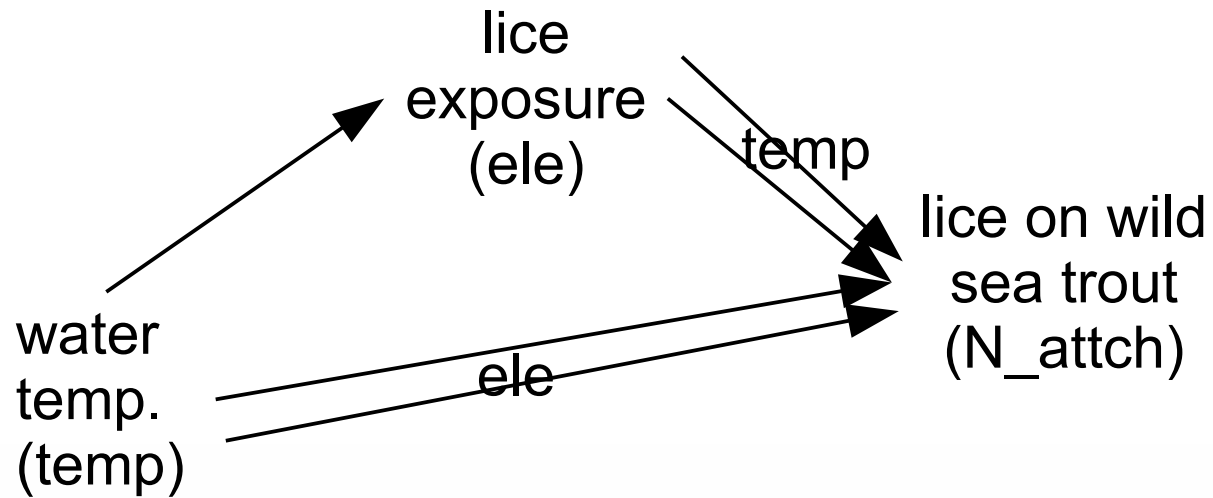
Parasitic sea louse infestations on wild sea trout: separating the roles of fish farms and temperature

Knut W. Vollset, Lars Qviller, Bjørnar Skår, Bjørn T. Barlaup and Ian Dohoo

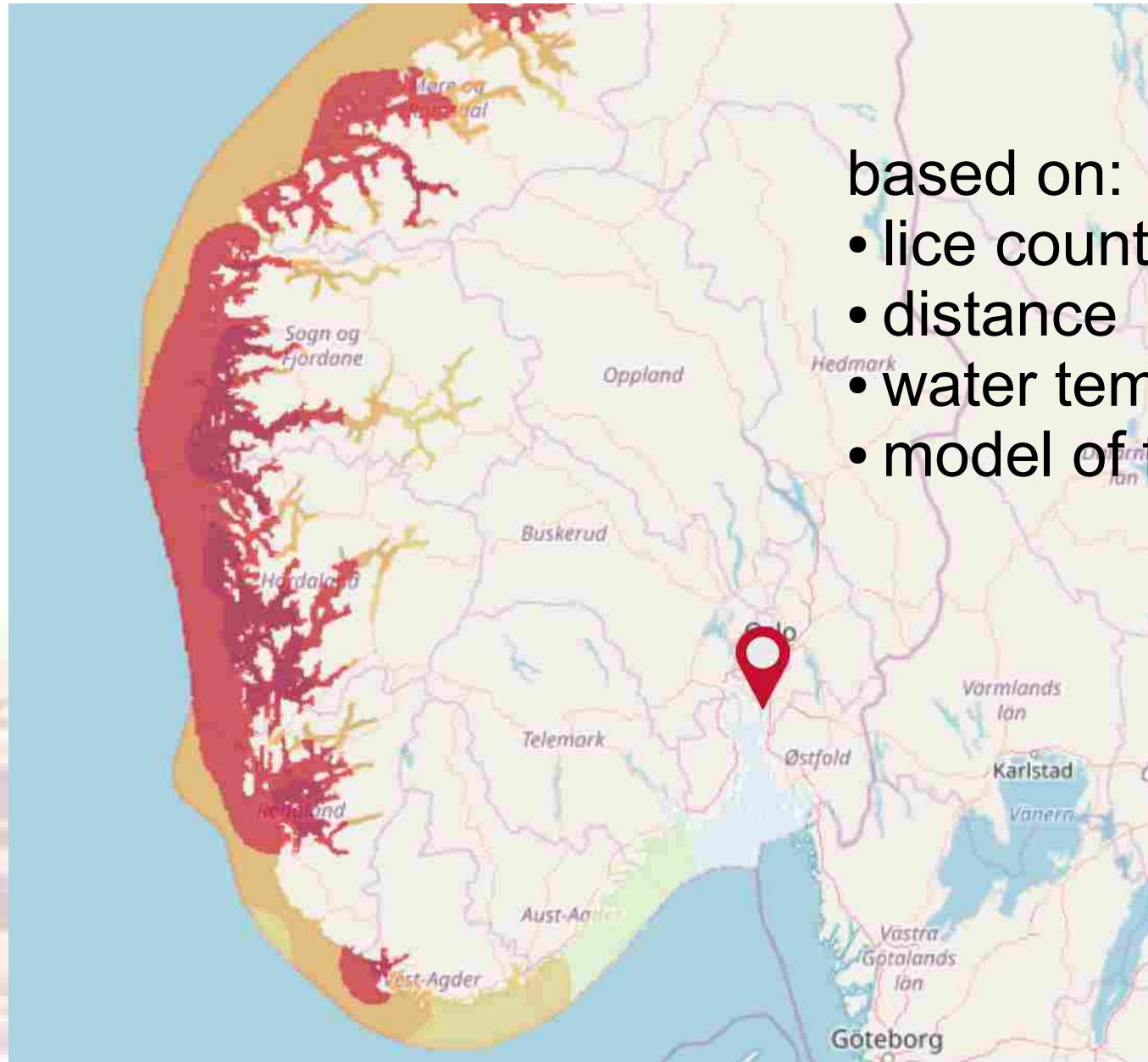
Parasites and Vectors, 2018 Nov 29;11(1):609

COVER

Motivating Example



e/e – Estimated lice exposure



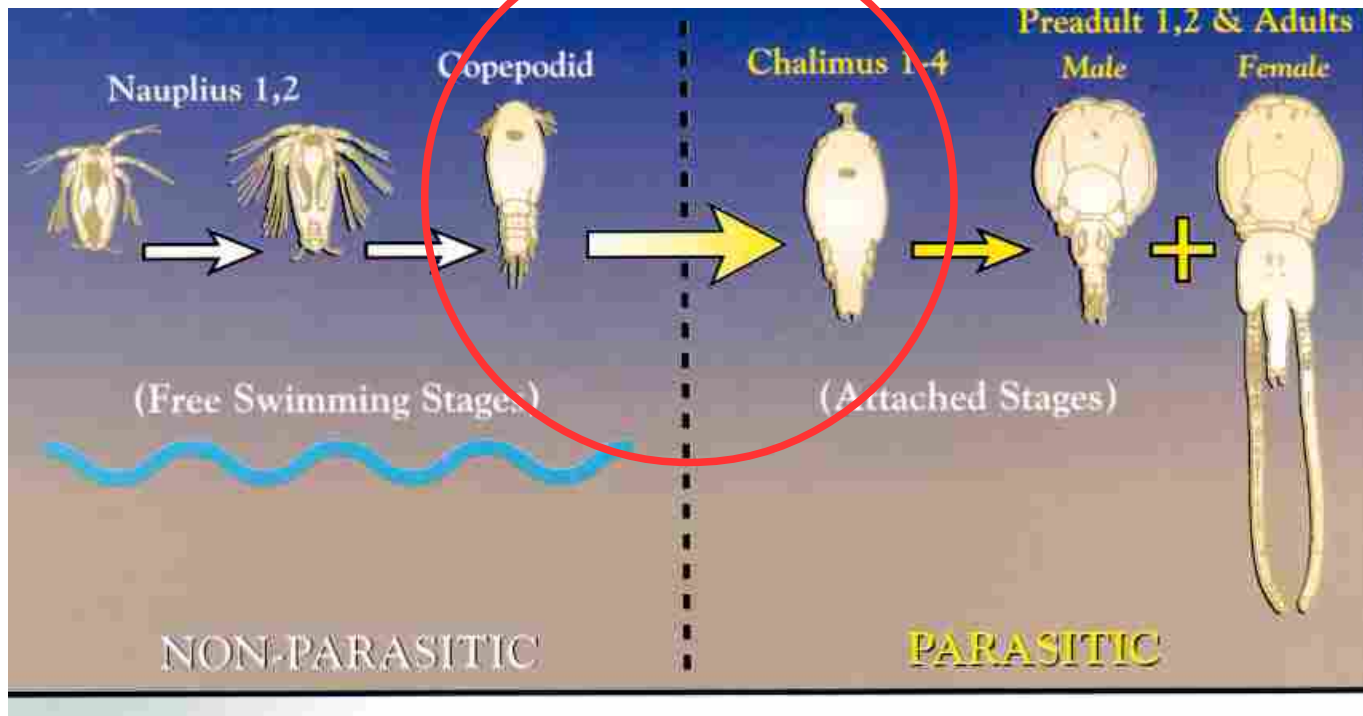
based on:

- lice counts on fish farms
- distance
- water temperature
- model of fecundity

Variables

Variable	mean	min	max
temp	9.83	5.96	13.84
ele	14.02	9.22	17.44
N_attch	24.7	0	770
N_mob	11.8	0	105
Standardized Variables			
temp	0	-1.93	2.00
ele	0	-2.28	1.62
N_attch	0	-1.44	2.59
N_mob	0	-1.42	2.06

Attached Lice



Regression - ZINB

	Coefficient	P	95% Confidence Interval	
<hr/>				
negative binomial				
temp	-0.166	0.073	-0.348	0.016
ele	0.909	0.000	0.703	1.114
temp*ele	0.803	0.000	0.614	0.991
ele2	-0.545	0.000	-0.716	-0.374
intercept	2.960	0.000	2.805	3.115
alpha	1.074		0.877	1.315
zero inflation				
ele	-1.016	0.000	-1.398	-0.634
intercept	-2.006	0.000	-2.473	-1.538

Regression - ZINB

	Coefficient	P	95% Confidence Interval	
<hr/>				
negative binomial				
temp	-0.166	0.073	-0.348	0.016
ele	0.909	0.000	0.703	1.114
temp*ele	0.803	0.000	0.614	0.991
ele2	-0.545	0.000	-0.716	-0.374
intercept	2.960	0.000	2.805	3.115
alpha	1.074		0.877	1.315
zero inflation				
ele				
intercept				

- **alpha ≈ 1 , variance = $\mu + \mu^2$**
- **variance much larger than Poisson model**
- **rises quickly with high counts**

Regression - ZINB

	Coeficient	P	95% Confidence Interval	
<u>negative binomial</u>				
temp	-0.166	0.073	-0.348	0.016
ele	0.909	0.000	0.703	1.114
temp*ele	0.803	0.000	0.614	0.991
ele2	-0.545	0.000	-0.716	-0.374
intercept	2.960	0.000	2.805	3.115
alpha				
<u>zero inflation</u>				
ele				
intercept	-2.006	0.000	-2.473	-1.538

- **ele:**
- **quadratic relationship**
- **interaction with temp**

Regression - ZINB

	Coefficient	P	95% Confidence Interval	
<u>negative binomial</u>				
temp	-0.166	0.073	-0.348	0.016
ele	0.909	0.000	0.703	1.114
temp*ele	0.803	0.000	0.614	0.991
ele2	-0.545	0.000	-0.716	-0.374
intercept	2.960	0.000	2.805	3.115
alpha	1.074		0.877	1.315
<u>zero inflation</u>				
ele	-1.016	0.000	-1.398	-0.634
intercept	-2.006	0.000	-2.473	-1.538

- LR test comparing NB and ZINB highly sig.
- ele only factor affecting zero inflation
 - $p(\text{zero})$ goes down linearly with ele

COVER

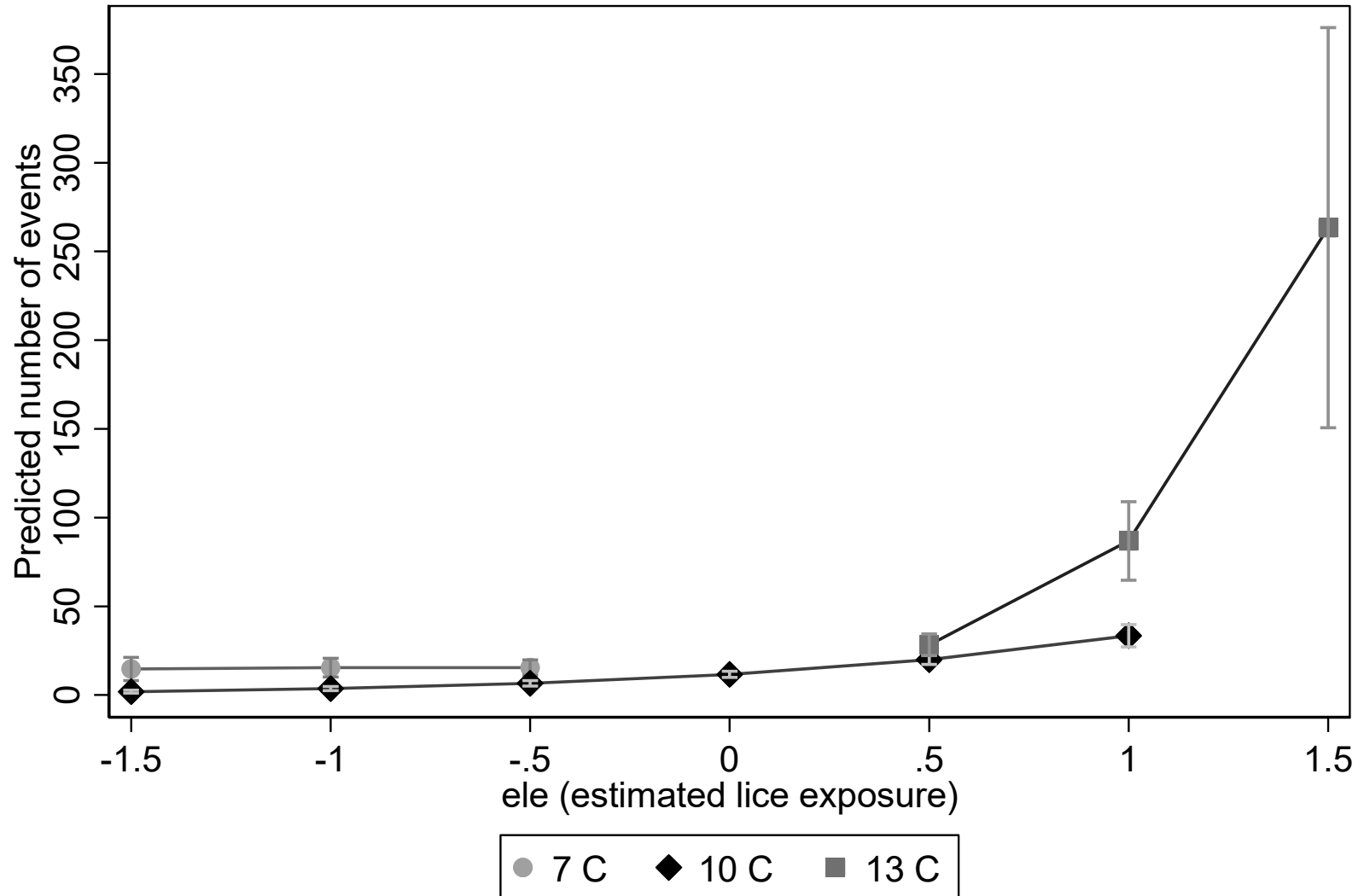
Regression - ZINB

	Coefficient	P	95% Confidence Interval	
<u>negative binomial</u>				
temp	-0.166	0.073	-0.348	0.016
ele	0.909	0.000	0.703	1.114
temp*ele	0.000	0.000	0.000	0.000
intercept	1.017	0.000	0.000	1.017
<u>zero inflation</u>				
ele	-1.016	0.000	-1.398	-0.634
intercept	-2.006	0.000	-2.473	-1.538

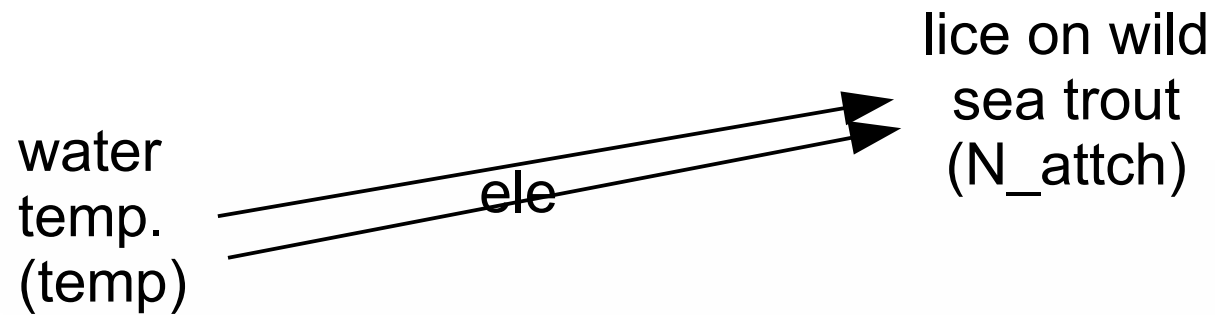
- at average levels of ele, temp only borderline sig. and negative
- evidence of limited direct effect ?

Marginal Estimates

Marginal Estimates - ZINB model

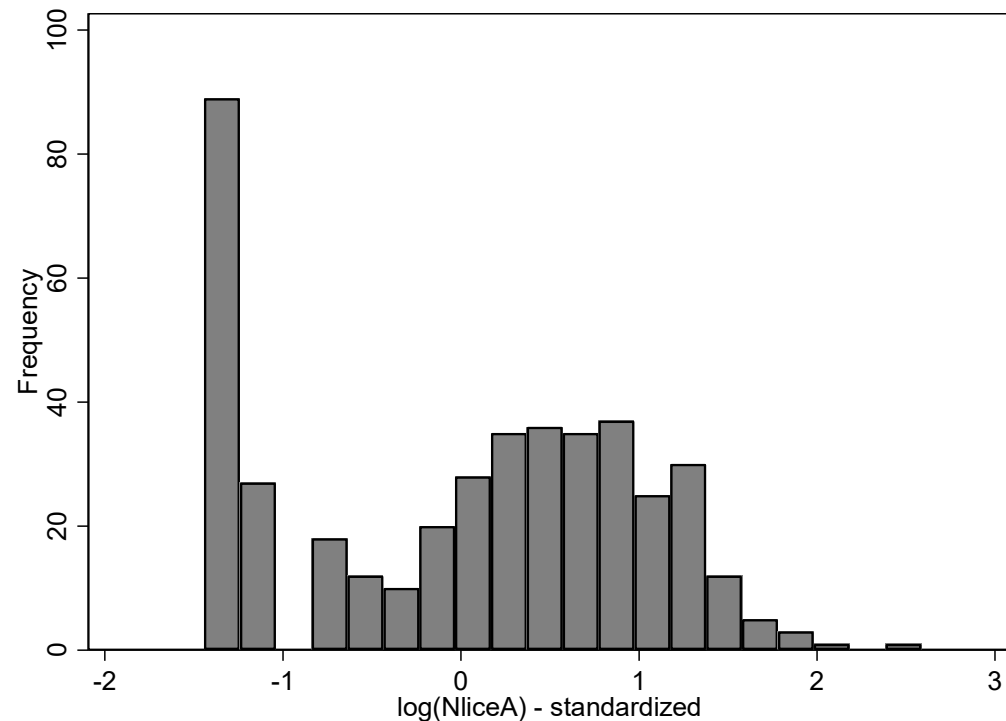


Motivating Example



ZINB vs linear regression

- no software for mediation analysis based on NB regression
- NB regression models $\log(\text{count})$
- would a linear model of $\log(\text{count})$ suffice ?



ZINB vs linear regression

Variable	ZINB	Linear
temp	-0.206*	-0.103
ele	1.0866***	1.084***
ele2	-0.662***	-0.430***
temp*ele	0.815***	0.688***
Intercept	2.871***	1.921***

* P<0.05 ** P<0.01 *** P<0.001

correlation of predicted values: 0.993

Mediation Analysis

- effect of *temp*
 - is it mediated through *ele* ?
 - allow for interaction between *temp* and *ele*
- Stata: - medeff-
 - user specifies change in *temp* to consider
- R: - medflex-
 - results for a 1 SD change in *temp*

Direct Effects

effect of temp that are NOT mediated through ele

Effect	Estimate	SE (signif)	Interpretation
Pure direct effect	0.007	0.060	the increase in <i>N_attch</i> brought about by a 1 SD increase in <i>temp</i> with <i>ele</i> held constant at an average temp
Total direct effect	0.156	0.051**	the increase in <i>N_attch</i> brought about by a 1 SD increase in <i>temp</i> with <i>ele</i> held constant at the level resulting from that 1 SD increase in <i>temp</i>

* P<0.05 ** P<0.01 *** P<0.001

Indirect Effects

effect of temp that ARE mediated through ele

Effect	Estimate	SE (signif)	Interpretation
Pure indirect effect	0.418	0.047***	the increase in <i>N_attach</i> brought about by increasing <i>ele</i> by the amount that would result from a 1 SD increase in <i>temp</i> , while holding <i>temp</i> constant at an average <i>temp</i>
Total indirect effect	0.567	0.073***	the increase in <i>N_attach</i> brought about by increasing <i>ele</i> by an amount that would result from 1 SD increase in <i>temp</i> , while holding <i>temp</i> constant at that elevated level

* P<0.05 ** P<0.01 *** P<0.001

% mediated

- total direct effect = 0.156
- total indirect effect = 0.567
- total effect = 0.723
 - a 1 SD increase in *temp* brings about an increase of 0.723 in *N_attch*
- % of total effect mediated through *e/e* = 78.4%
 - almost 80% of the effect of rising water temperature results from the impact of water temperature on infestation pressure (*e/e*)

Mediation Analysis

- for attached lice
- rising water temperatures
 - interaction with ele
 - small positive direct effect
 - large positive indirect effect
- overall almost 80% of *temp* effect mediated through *ele*

R: -medflex- vs -mediation-

- after completing this project ... discovered -mediation-
 - much easier to use and understand
 - handles much wider range of models
 - including NB
 - doesn't give direct access to counterfactuals
- comparison of:
 - linear model on log scale
 - NB regression

R: -medflex- vs -mediation-

Proportion mediated		
Model	linear (log) -mdeflex-	NB -mediation-
mediator - ele	63%	65%
mediator – ele, ele ²	61%	59%
interaction between temp and ele	78%	84%

Terminology – no interaction

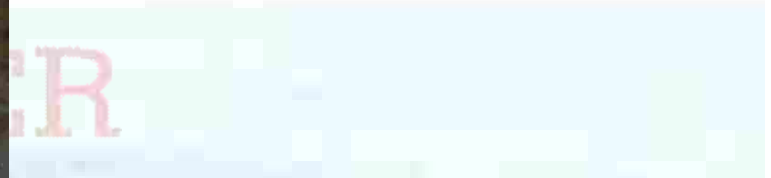
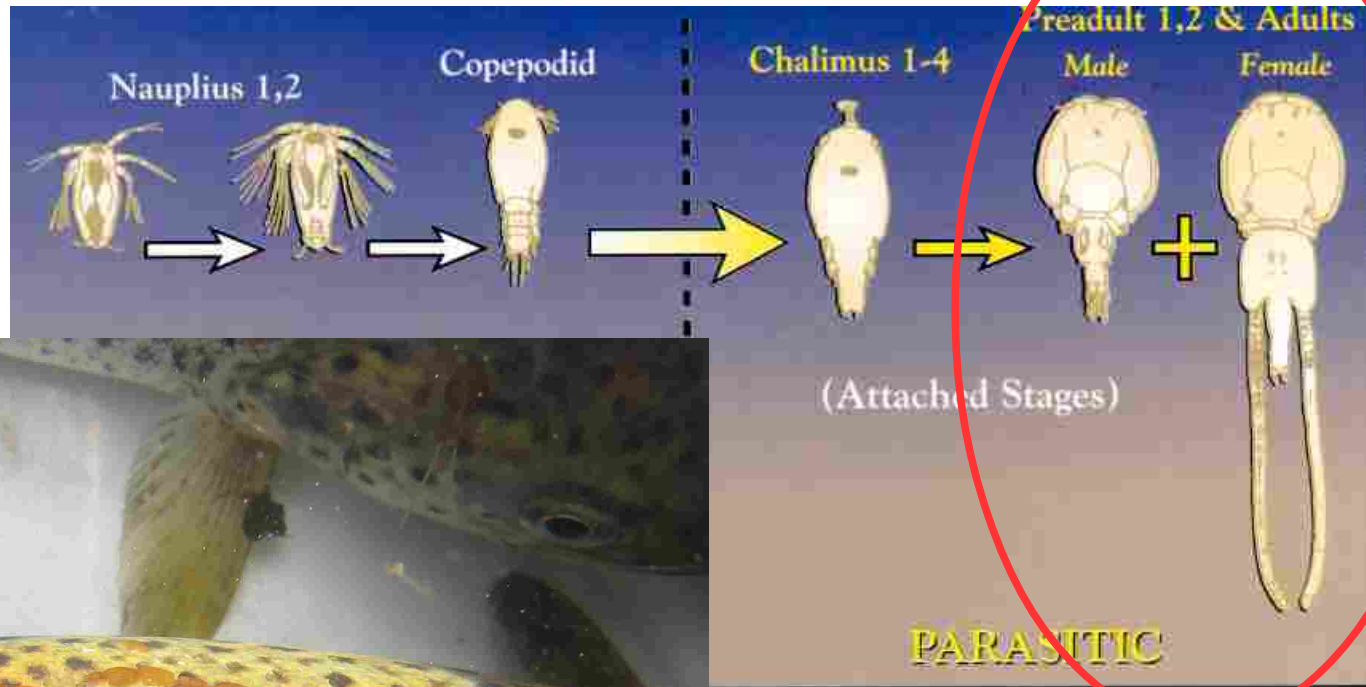
Stata	-medflex-	-medflex- decomposition	-mediation-
ACME	varname1	natural indirect effect	ACME
direct effect	varname0	natural direct effect	ADE
total effect	-	total effect	total effect
% of total effect mediated	-	-	propn. mediated

Terminology – interaction

Stata	-medflex-	-medflex- decomposition	-mediation-
ACME1	presented as model with:	total indirect	ACME (treatment)
ACME0	varname1	pure indirect	ACME (control)
direct effect 1	varname0	total direct	ADE (treatment)
direct effect 0	interaction term	pure direct	ADE (control)
total effect		total effect	total effect
avg. mediated		-	ACME (average)
avg. direct effect		-	ADE (average)
% of total effect mediated		-	Prop. mediated (average)



Mobile Lice



Regression - NB

	Coefficient	P	95% Confidence Interval	
temp	-0.458	0.000	-0.666	-0.250
temp ²	-0.206	0.010	-0.364	-0.049
ele	0.626	0.000	0.446	0.807
ele ²	0.189	0.007	0.051	0.328
intercept	2.295	0.000	2.119	2.471
alpha	1.610		1.387	1.868

- no evidence of variance inflation

Regression - NB

	Coefficient	P	95% Confidence Interval	
temp	-0.458	0.000	-0.666	-0.250
temp ²	-0.206	0.010	-0.364	-0.049
ele	0.626	0.000	0.446	0.807
ele ²	0.189	0.007	0.051	0.328
intercept	2.295	0.000	2.119	2.471
alpha	1.610		1.387	1.868

- alpha ≈ 1.6 , variance = $\mu + 2.6(\mu^2)$
- variance much larger than Poisson model
- rises quickly with high counts

Regression - NB

	Coefficient	P	95% Confidence Interval	
temp	-0.458	0.000	-0.666	-0.250
temp ²	-0.206	0.010	-0.364	-0.049
ele	0.626	0.000	0.446	0.807
ele ²				
intercept				
alpha	1.610		1.387	1.868

- temp effect is quadratic
- lower mobile lice counts with increasing temperature

Regression - NB

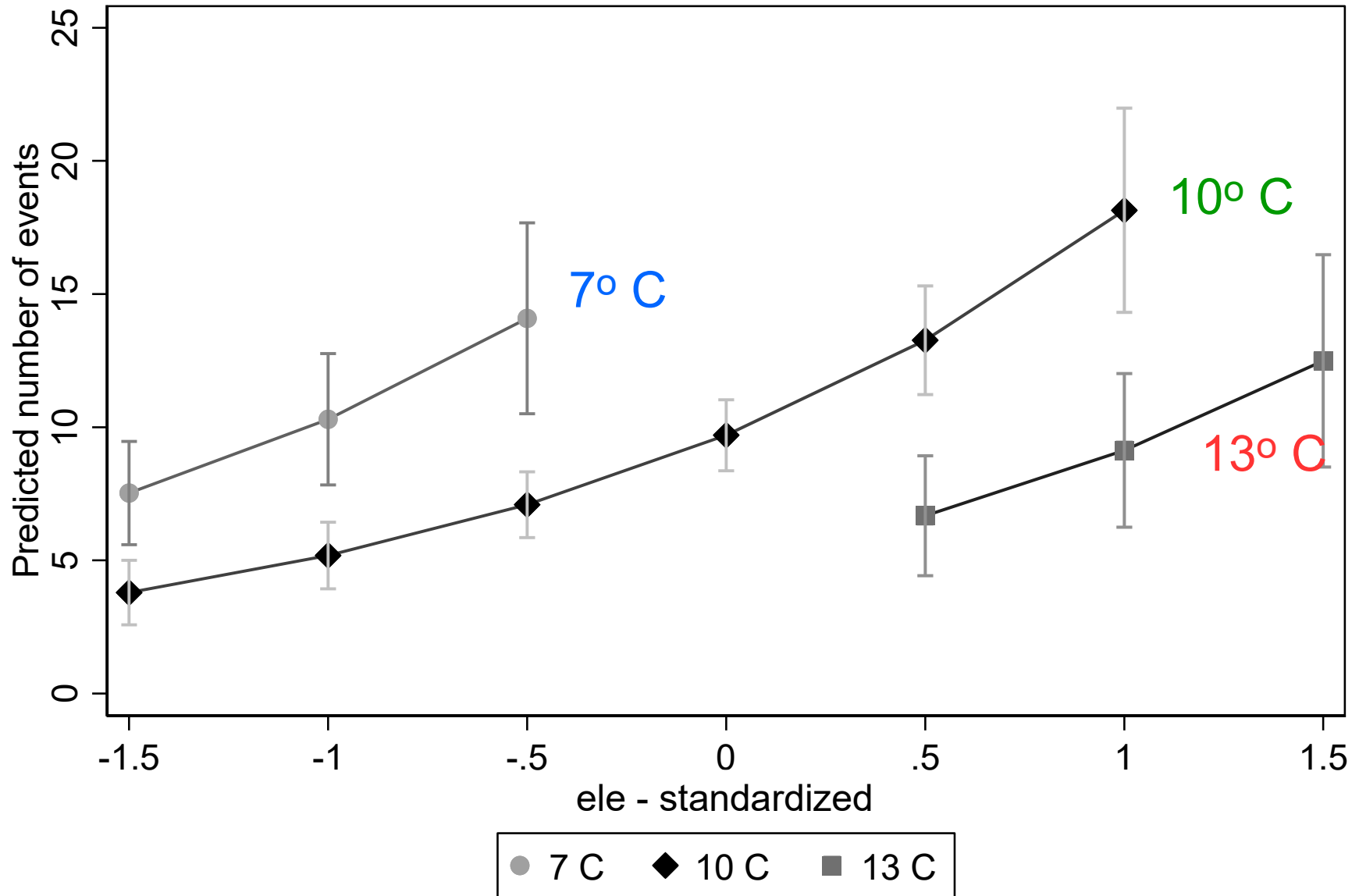
	Coefficient	P	95% Confidence Interval	
temp	-0.458	0.000	-0.666	-0.250
temp ²	-0.206	0.010	-0.364	-0.049
ele	0.626	0.000	0.446	0.807
ele ²	0.189	0.007	0.051	0.328
intercept	2.295	0.000	2.119	2.471

alpha

- ele effect is quadratic
- higher mobile lice counts with increasing infestation pressure

Marginal Effects

Adult lice - nb model



Mediation Analysis

direct and indirect effects of *temp*

Effect	Estimate	SE (signif)	Interpretation
Natural direct effect	-0.43	0.054***	the increase in N_mob brought about by a 1 SD increase in <i>temp</i> with <i>ele</i> held constant at value seen at average <i>temp</i>
Natural indirect effect	0.34	0.038***	the increase in N_mob brought about by increasing <i>ele</i> by the amount that would result from a 1 SD increase in <i>temp</i> while holding <i>temp</i> constant at an average <i>temp</i>
Total effect	-0.1	0.046*	the overall decrease in N_mob brought about by increasing <i>temp</i> by 1 SD

* $P < 0.05$ ** $P < 0.01$ *** $P < 0.001$

Mediation Analysis

- for mobile lice
- rising water temperatures
 - direct effect = lower lice counts
 - indirect effect = higher lice counts
 - overall = borderline significant reduction in counts with rising temperatures
- counts rose with increasing e/e at all temperatures



ISVVEE 16

HALIFAX 2021

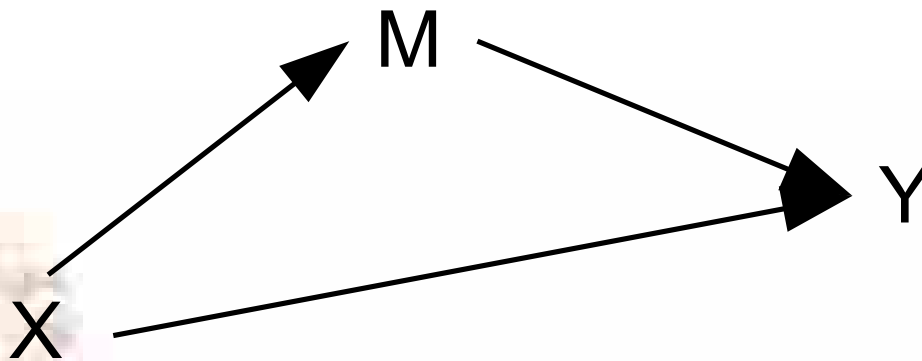


... more technical stuff

- Stata /R terminology
- a “peek under the hood”
 - looking at the simulated counterfactual data

A peek under the hood

- assume simple model with:
 - Y = continuous outcome
 - X = dichotomous factor of interest
 - M = dichotomous mediator



Ordinary regression model

$$Y = \beta_c + \beta_0 X + \beta_1 M$$

- β_c = intercept (not relevant)
- β_0 = (direct) effect of X holding M constant
- β_1 = (direct) effect of M holding X constant

Mediation model

$$Y^c = \beta_c + \beta_0 X_0 + \beta_1 X_1$$

- X_0 = a synthesized X value – taken from range of X values
- X_1 = original X value
- Y^c = counterfactual estimate of Y – based on values of X_0 and M
 - β_c = intercept (not relevant)
 - β_0 = (direct) effect of X
 - β_1 = (indirect) effect of X mediated through M



ISVEE 16

HALIFAX 2021

COVER